

Marking Scheme
Strictly Confidential
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Secondary School Supplementary Examination, July- 2023
MATHEMATICS PAPER CODE 30/C/B

General Instructions: -

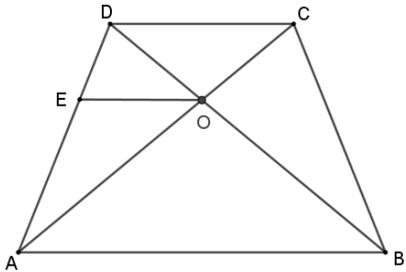
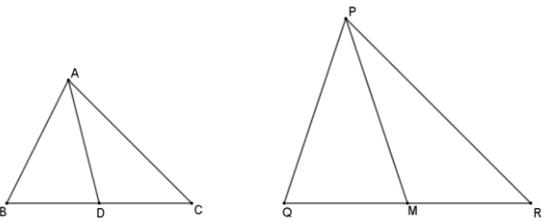
1	You are aware that evaluation is the most important process in the actual and correct assessment of the candidates. A small mistake in evaluation may lead to serious problems which may affect the future of the candidates, education system and teaching profession. To avoid mistakes, it is requested that before starting evaluation, you must read and understand the spot evaluation guidelines carefully.
2	“Evaluation policy is a confidential policy as it is related to the confidentiality of the examinations conducted, Evaluation done and several other aspects. Its’ leakage to public in any manner could lead to derailment of the examination system and affect the life and future of millions of candidates. Sharing this policy/document to anyone, publishing in any magazine and printing in News Paper/Website etc may invite action under various rules of the Board and IPC.”
3	Evaluation is to be done as per instructions provided in the Marking Scheme. It should not be done according to one’s own interpretation or any other consideration. Marking Scheme should be strictly adhered to and religiously followed. However, while evaluating, answers which are based on latest information or knowledge and/or are innovative, they may be assessed for their correctness otherwise and due marks be awarded to them. In class-X, while evaluating two competency-based questions, please try to understand given answer and even if reply is not from marking scheme but correct competency is enumerated by the candidate, due marks should be awarded.
4	The Marking scheme carries only suggested value points for the answers. These are in the nature of Guidelines only and do not constitute the complete answer. The students can have their own expression and if the expression is correct, the due marks should be awarded accordingly.
5	The Head-Examiner must go through the first five answer books evaluated by each evaluator on the first day, to ensure that evaluation has been carried out as per the instructions given in the Marking Scheme. If there is any variation, the same should be zero after deliberation and discussion. The remaining answer books meant for evaluation shall be given only after ensuring that there is no significant variation in the marking of individual evaluators.
6	Evaluators will mark (✓) wherever answer is correct. For wrong answer CROSS ‘X’ be marked. Evaluators will not put right (✓) while evaluating which gives an impression that answer is correct and no marks are awarded. This is most common mistake which evaluators are committing.
7	If a question has parts, please award marks on the right-hand side for each part. Marks awarded for different parts of the question should then be totaled up and written in the left-hand margin and encircled. This may be followed strictly.
8	If a question does not have any parts, marks must be awarded in the left-hand margin and encircled. This may also be followed strictly.
9	<u>In Q1-Q20, if a candidate attempts the question more than once (without canceling the previous attempt), marks shall be awarded for the first attempt only and the other answer scored out with a note “Extra Question”.</u>
10	<u>In Q21-Q38, if a student has attempted an extra question, answer of the question deserving more marks should be retained and the other answer scored out with a note “Extra Question”.</u>

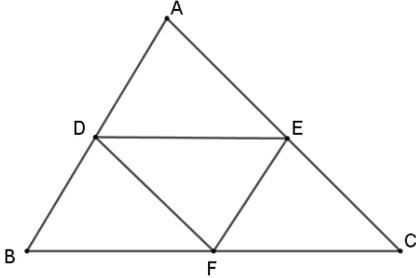
11	No marks to be deducted for the cumulative effect of an error. It should be penalized only once.
12	A full scale of marks _____ (example 0 to 80/70/60/50/40/30 marks as given in Question Paper) has to be used. Please do not hesitate to award full marks if the answer deserves it.
13	Every examiner has to necessarily do evaluation work for full working hours i.e., 8 hours every day and evaluate 20 answer books per day in main subjects and 25 answer books per day in other subjects (Details are given in Spot Guidelines). This is in view of the reduced syllabus and number of questions in question paper.
14	<p>Ensure that you do not make the following common types of errors committed by the Examiner in the past:-</p> <ul style="list-style-type: none"> ● Leaving answer or part thereof unassessed in an answer book. ● Giving more marks for an answer than assigned to it. ● Wrong totaling of marks awarded on an answer. ● Wrong transfer of marks from the inside pages of the answer book to the title page. ● Wrong question wise totaling on the title page. ● Wrong totaling of marks of the two columns on the title page. ● Wrong grand total. ● Marks in words and figures not tallying/not same. ● Wrong transfer of marks from the answer book to online award list. ● Answers marked as correct, but marks not awarded. (Ensure that the right tick mark is correctly and clearly indicated. It should merely be a line. Same is with the X for incorrect answer.) ● Half or a part of answer marked correct and the rest as wrong, but no marks awarded.
15	While evaluating the answer books if the answer is found to be totally incorrect, it should be marked as cross (X) and awarded zero (0) Marks.
16	Any un assessed portion, non-carrying over of marks to the title page, or totaling error detected by the candidate shall damage the prestige of all the personnel engaged in the evaluation work as also of the Board. Hence, in order to uphold the prestige of all concerned, it is again reiterated that the instructions be followed meticulously and judiciously.
17	The Examiners should acquaint themselves with the guidelines given in the “ Guidelines for spot Evaluation ” before starting the actual evaluation.
18	Every Examiner shall also ensure that all the answers are evaluated, marks carried over to the title page, correctly totaled and written in figures and words.
19	The candidates are entitled to obtain photocopy of the Answer Book on request on payment of the prescribed processing fee. All Examiners/Additional Head Examiners/Head Examiners are once again reminded that they must ensure that evaluation is carried out strictly as per value points for each answer as given in the Marking Scheme.

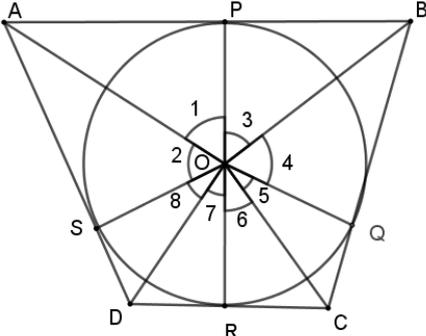
4.	The pair of equations $x = a$ and $y = b$ represent the lines which are : (a) parallel (b) intersecting at (b, a) (c) coincident (d) intersecting at (a, b)	
Ans.	(d) intersecting at (a,b)	1
5.	If one equation of a pair of dependent equations is $-3x + 5y = 4$, then the second equation can be : (a) $6x + 10y = 8$ (b) $9x - 15y + 12 = 0$ (c) $-9x + 15y = -12$ (d) $-6x - 10y = 8$	
Ans.	(b) $9x - 15y + 12 = 0$	1
6.	If one root of the equation $2x^2 - 5x + (\lambda - 4) = 0$ be the reciprocal of the other, then the value of λ is : (a) 5 (b) 4 (c) 6 (d) 8	
Ans.	(c) 6	1
7.	The 4 th term from the end of an AP $-11, -8, -5, \dots, 49$ is : (a) 40 (b) 37 (c) 43 (d) 58	
Ans.	(a) 40	1
8.	The perimeters of two similar triangles are 42 cm and 35 cm respectively. If one side of the first triangle is 12 cm, then the corresponding side of the second triangle is : (a) 5 cm (b) 7.5 cm (c) 8 cm (d) 10 cm	
Ans.	(d) 10 cm	1

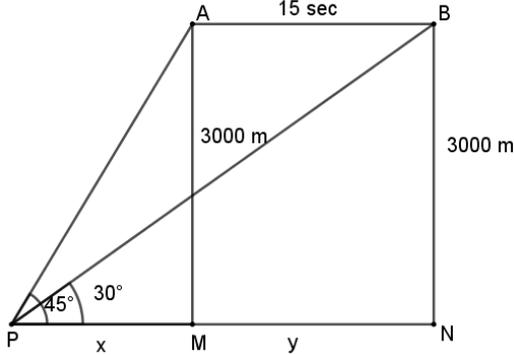
	$y = \frac{5(-4)+1(-6)}{6} = -\frac{13}{2}$ $\therefore \text{point of intersection is } (0, -\frac{13}{2})$	$\frac{1}{2}$ $\frac{1}{2}$
24.	<p>If $\tan A = 1$ and $\tan B = \sqrt{3}$, then evaluate ;</p> $\cos A \cos B + \sin A \sin B.$	
Ans.	$A = 45^\circ, B = 60^\circ$ $\cos A \cos B + \sin A \sin B$ $= \frac{1}{\sqrt{2}} \cdot \frac{1}{2} + \frac{1}{\sqrt{2}} \cdot \frac{\sqrt{3}}{2} = \frac{\sqrt{3}+1}{2\sqrt{2}}$	$\frac{1}{2}+\frac{1}{2}$ 1
25(a).	<p>Prove that</p> $\frac{1 - \cos \theta}{1 + \cos \theta} = (\cot \theta - \operatorname{cosec} \theta)^2$	
Ans.	$\text{LHS} = \frac{1 - \cos \theta}{1 + \cos \theta} \times \frac{1 - \cos \theta}{1 - \cos \theta}$ $= \frac{(1 - \cos \theta)^2}{\sin^2 \theta}$ $= (\operatorname{cosec} \theta - \cot \theta)^2 = \text{RHS}$	1 $\frac{1}{2}$ $\frac{1}{2}$
	OR	
25(b).	<p>Prove that</p> $\frac{\tan A}{1 - \cot A} + \frac{\cot A}{1 - \tan A} = 1 + \sec A \operatorname{cosec} A$	
Ans.	<p>Getting $\frac{\sin^2 A}{\cos A(\sin A - \cos A)} + \frac{\cos^2 A}{\sin A(\cos A - \sin A)}$</p> $= \frac{\sin^3 A - \cos^3 A}{\sin A \cos A(\sin A - \cos A)} = \frac{\sin^2 A + \cos^2 A + \sin A \cos A}{\sin A \cos A}$ $= 1 + \sec A \operatorname{cosec} A = \text{RHS}$	1 $\frac{1}{2}$ $\frac{1}{2}$

SECTION C		
This section comprises of Short Answer (SA) type questions of 3 marks each.		
26.	Prove that $\sqrt{5}$ is an irrational number.	
Ans.	<p>Let $\sqrt{5}$ be a rational number. $\therefore \sqrt{5} = \frac{p}{q}$, where $q \neq 0$ and let p & q be co-primes. $5q^2 = p^2 \Rightarrow p^2$ is divisible by 5 $\Rightarrow p$ is divisible by 5 $\Rightarrow p = 5a$, where 'a' is some integer ----- (i) $25a^2 = 5q^2 \Rightarrow q^2 = 5a^2 \Rightarrow q^2$ is divisible by 5 $\Rightarrow q$ is divisible by 5 $\Rightarrow q = 5b$, where 'b' is some integer ----- (ii) (i) and (ii) leads to contradiction as 'p' and 'q' are co-primes. $\therefore \sqrt{5}$ is an irrational number.</p>	<p>1</p> <p>1</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p>
27.	A boat goes 30 km upstream and 44 km downstream in 10 hours. It goes 40 km upstream and 55 km downstream in 13 hours. Find the speed of the boat in still water and that of the stream.	
Ans.	<p>Let the speed of the boat be x km/h and the speed of the stream be y km/h A.T.Q $\frac{30}{x-y} + \frac{44}{x+y} = 10$; $\frac{40}{x-y} + \frac{55}{x+y} = 13$ $\Rightarrow x + y = 11, x - y = 5$ $\Rightarrow x = 8, y = 3$ \therefore Speed of boat = 8 km/h Speed of stream = 3 km/h</p>	<p>1</p> <p>1</p> <p>1</p>

28.	<p>ABCD is a trapezium in which $AB \parallel DC$ and its diagonals AC and BD intersect at O. Show that $\frac{OA}{OB} = \frac{OC}{OD}$.</p>	
Ans.	 <p>Draw $OE \parallel CD$</p> $\Rightarrow \frac{DE}{AE} = \frac{OD}{OB}$ <p>Also $\frac{DE}{AE} = \frac{OC}{OA}$</p> $\Rightarrow \frac{OD}{OB} = \frac{OC}{OA} \Rightarrow \frac{OA}{OB} = \frac{OC}{OD}$	<p>1</p> <p>1</p> <p>1</p>
29(a).	<p>Sides AB and BC and the median AD of a triangle ABC are respectively proportional to the sides PQ and QR and the median PM of ΔPQR. Show that $\Delta ABC \sim \Delta PQR$.</p>	
Ans.	 <p>Given $\frac{AB}{PQ} = \frac{BC}{QR} = \frac{AD}{PM} \Rightarrow \frac{AB}{PQ} = \frac{2BD}{2QM} = \frac{AD}{PM}$</p> <p>$\therefore \Delta ABD \sim \Delta PQM \Rightarrow \angle B = \angle Q$</p> <p>Now, $\frac{AB}{PQ} = \frac{BC}{QR}$ and $\angle B = \angle Q \Rightarrow \Delta ABC \sim \Delta PQR$</p>	<p>1</p> <p>1</p> <p>1</p>
OR		
29(b).	<p>Prove that each of the four triangles formed by joining the mid-points of the sides of a triangle are similar to the original triangle.</p>	

<p>Ans.</p>	 <p>In $\triangle ABC$ and $\triangle DEF$</p> <p>$\angle A = \angle F$ (Opposite angles of \parallelgm)</p> <p>Also $\frac{AB}{EF} = \frac{2}{1} = \frac{AC}{DF} \Rightarrow \triangle ABC \sim \triangle FED$</p> <p>Similarly, we can prove other pairs</p>	<p>1</p> <p>1</p> <p>1</p>
<p>30(a).</p>	<p>A horse is tied with a rope of length 6 m at the corner of a square grassy lawn of side 20 m. If the length of the rope is increased by 5.5 m, find the increase in area of the lawn in which the horse can graze.</p>	
<p>Ans.</p>	<p>Increase in Area = $\pi[(11.5)^2 - 6^2] \frac{90}{360}$ $= \frac{22}{7} \times \frac{175}{10} \times \frac{55}{10} \times \frac{1}{4} = 75.62$ Hence increase in area is 75.62 m^2</p>	<p>1½</p> <p>1½</p>
OR		
<p>30(b).</p>	<p>A chord of a circle of radius 14 cm makes a right angle at the centre of the circle. Find the area of the minor segment.</p>	
<p>Ans.</p>	<p>Area of segment = $\frac{22}{7} \times 14 \times 14 \times \frac{90}{360} - \frac{1}{2} \times 14 \times 14$ $= 154 - 98 = 56$ Hence area of segment = 56 cm^2</p>	<p>1½</p> <p>1½</p>
<p>31.</p>	<p>Three different coins are tossed simultaneously. Find the probability of getting :</p> <p>(i) At least one head, (ii) At most two heads.</p>	

Ans.	(i) $P(\text{at least one head}) = \frac{7}{8}$ (ii) $P(\text{at most two heads}) = \frac{7}{8}$	1½ 1½
SECTION D This section comprises of Long Answer (LA) type questions of 5 marks each.		
32(a).	Solve the equation for x : $-4 + (-1) + 2 + \dots + x = 437$.	
Ans.	$S_n = 437, a = -4, d = 3, a_n = x$ $437 = \frac{n}{2}[-8 + (n-1)3]$ $\Rightarrow 3n^2 - 11n - 874 = 0$ or $(3n + 46)(n - 19) = 0$ $\Rightarrow n = 19$ $x = a_{19} = -4 + 18(3) = 50$	1 1 1 1 1
OR		
32(b).	The sum of first n terms of an AP is $5n^2 + 3n$. If its n^{th} term is 168, find n . Also, find the 20^{th} term of the AP.	
Ans.	$S_n = 5n^2 + 3n \Rightarrow S_1 = 8 \Rightarrow a = 8$ $S_2 = a_1 + a_2 = 26 \Rightarrow a_2 = 18$ $\Rightarrow d = 18 - 8 = 10$ $a_n = 168 = 8 + (n-1)10 \Rightarrow n = 17$ $a_{20} = 8 + 190 = 198$	1 1½ 1½ 1
33(a).	Prove that opposite sides of a quadrilateral circumscribing a circle subtend supplementary angles at the centre of the circle.	
Ans.		

	<p>$AP = AS$, so $\angle 1 = \angle 2$ Similarly, $\angle 3 = \angle 4$ $\angle 7 = \angle 8$ $\angle 6 = \angle 5$ $\Rightarrow (\angle 1 + \angle 3) + (\angle 6 + \angle 7) = (\angle 2 + \angle 8) + (\angle 4 + \angle 5)$ $\Rightarrow (\angle AOB + \angle COD) = (\angle AOD + \angle BOC) = 180^\circ$ \therefore Angles subtended by AB and CD or AD and BC are supplementary</p>	<p>2 1 1 1</p>
OR		
33(b).	Prove that the lengths of the tangents drawn from an external point to a circle are equal.	
Ans.	Correct Given, To prove and Construction Correct Proof	2 3
34.	<p>The angle of elevation of an aeroplane from a point on the ground is 45°. After a flight of 15 seconds, the elevation changes to 30°. If the aeroplane is flying at a constant height of 3000 meters, find the speed of the aeroplane in km/h.</p> <p>[Take $\sqrt{3} = 1.732$]</p>	
Ans.	 <p>$\frac{3000}{x} = \tan 45^\circ = 1 \Rightarrow x = 3000 \text{ m}$</p>	1

	$\frac{3000}{x+y} = \tan 30^\circ = \frac{1}{\sqrt{3}} \Rightarrow 3000 + y = 3000\sqrt{3}$ $y = 3000(\sqrt{3} - 1) = 3000(0.732) = 2196 \text{ m}$ $\text{Speed} = \frac{2196}{15} = 146.4 \text{ m/s}$	<p>1½</p> <p>1½</p> <p>1</p>																				
35.	<p>Find the mean and the median for the following frequency distribution :</p> <table border="1" data-bbox="302 550 873 1153"> <thead> <tr> <th><i>Class</i></th> <th><i>Frequency</i></th> </tr> </thead> <tbody> <tr> <td>11 – 13</td> <td>7</td> </tr> <tr> <td>13 – 15</td> <td>6</td> </tr> <tr> <td>15 – 17</td> <td>9</td> </tr> <tr> <td>17 – 19</td> <td>13</td> </tr> <tr> <td>19 – 21</td> <td>20</td> </tr> <tr> <td>21 – 23</td> <td>5</td> </tr> <tr> <td>23 – 25</td> <td>4</td> </tr> </tbody> </table>	<i>Class</i>	<i>Frequency</i>	11 – 13	7	13 – 15	6	15 – 17	9	17 – 19	13	19 – 21	20	21 – 23	5	23 – 25	4					
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12	7	84	7																			
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16	9	144	22																			
18	13	234	35																			

	20	20	400	55	
	22	5	110	60	
	24	4	96	64	
	Total	64	1152		
	$\text{Mean} = \frac{1152}{64} = 18$				1
	Median group: 17-19				$\frac{1}{2}$
	$\text{Median} = 17 + \frac{32-22}{13} \times 2 = 17 + \frac{20}{13}$ $= 18.54$				1
					$\frac{1}{2}$
	SECTION E				
	This section comprises of 3 case-study based questions of 4 marks each.				
36.	<p style="text-align: center;">Case Study – 1</p> <p>In an auditorium, seats are arranged in rows and columns. The number of rows are equal to the number of seats in each row in the beginning. When the number of rows are doubled and the number of seats in each row is reduced by 10, the total number of seats increases by 300.</p> <p>Based on the above, answer the following questions :</p> <p>(a) Taking x as the number of rows in the beginning, represent the above situation by a quadratic equation. 1</p> <p>(b) (i) How many rows are there in the original arrangement? 2</p> <p style="text-align: center;">OR</p> <p>(ii) How many seats are there in the auditorium in the beginning? 2</p> <p>(c) How many seats are there in the auditorium after re-arrangement? 1</p>				

<p>Ans.</p>	<p>Let no. of rows be x = no. of seats in each row</p> <p>(a) $2x(x - 10) - x^2 = 300$</p> <p>Or $x^2 - 20x - 300 = 0$</p> <p>(b) (i) $(x - 30)(x + 10) = 0 \Rightarrow x = 30$</p> <p>OR</p> <p>(ii) $(x - 30)(x + 10) = 0 \Rightarrow x = 30$</p> <p style="text-align: center;">$\therefore x^2 = 900$</p> <p>(c) $900 + 300 = 1200$</p>	<p style="text-align: center;">1</p> <p style="text-align: center;">1+1=2</p> <p style="text-align: center;">1+1=2</p> <p style="text-align: center;">1</p>
<p>37.</p>	<p style="text-align: center;">Case Study – 2</p> <p>Morning assembly is an integral part of every school's schedule. In the assembly, students always stand in rows and columns and this makes a coordinate system.</p> <p>In a school, there are 200 students and they all assemble for prayer in 10 rows. 4 students are at A, B, C and D with the following positions of the coordinate system :</p> <p>A (3, 4), B (6, 7), C (9, 4) and D (6, 1).</p> <p>Based on the above, answer the following questions :</p> <p>(a) Find the distance between A and B. <i>1</i></p> <p>(b) Find the distance between C and D. <i>1</i></p> <p>(c) Show that ABCD forms a parallelogram. <i>2</i></p> <p style="text-align: center;">OR</p> <p>(c) Find the mid-point of the line segments AC and BD. <i>2</i></p>	

<p>Ans.</p>	<p>(a) $AB = \sqrt{(6-3)^2 + (7-4)^2} = 3\sqrt{2}$ units</p> <p>(b) $CD = \sqrt{(6-9)^2 + (1-4)^2} = 3\sqrt{2}$ units</p> <p>(c) (i) $AB = CD$</p> <p>$AD = \sqrt{(6-3)^2 + (1-4)^2} = 3\sqrt{2}$ units</p> <p>$BC = \sqrt{(9-6)^2 + (4-7)^2} = 3\sqrt{2}$ units</p> <p>$\Rightarrow AD = BC$</p> <p>\therefore ABCD is a gm</p> <p style="text-align: center;">OR</p> <p>(ii) mid-point of AC is (6,4)</p> <p>And mid-point of BD is (6,4)</p>	<p>1</p> <p>1</p> <p>1</p> <p>1</p> <p>1</p> <p>1</p>
<p>38.</p>	<p style="text-align: center;">Case Study – 3</p> <p>For the Kumbh Mela, Uttar Pradesh Government prescribed the following for the contractors to pitch the tents.</p> <p>Each tent must be of cylindrical base of radius 21 m and height 5 m, surmounted by a conical part of height 20 m. The cylindrical part must have a white coloured thick fabric costing ₹ 60 per square meter, while the conical part must have PVC coated blue fabric costing ₹ 70 per square meter.</p> <p>Based on the above information, answer the following questions :</p> <p>(a) How much blue PVC (in sq.m) is required and what will be its total cost ?</p> <p>(b) How much white fabric (in sq.m) is required and what will be its total cost ?</p>	<p>2</p> <p>2</p>
<p>Ans.</p>	<p>(a) $l = \sqrt{20^2 + 21^2} = \sqrt{841} = 29$ m</p> <p>CSA of conical part = $\pi r l = \frac{22}{7} \times 21 \times 29 = 1914 m^2$</p>	<p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p>

Cost = $1914 \times 70 = ₹ 133980$	1
(b) Surface Area of cylindrical part = $2 \times \frac{22}{7} \times 21 \times 5 = 660 m^2$	1
Cost = $660 \times 60 = ₹ 39600$	1